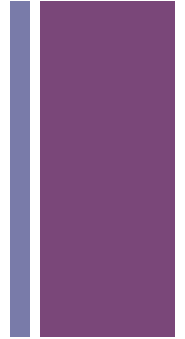


## BinarySearchTree Implementation

# + Efficient Dynamic Structure for Search?



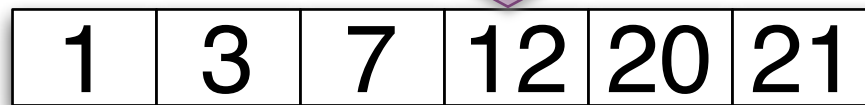
- What is a typical data structure used for search?
  - Sorted Array
- What if we want the structure to be dynamic?
  - Will a linked list work?
- How do we make the structure efficient?

# + Insert Into a Sorted Structure

- Insert 5 into...

(Search is fast, Insert requires shift)

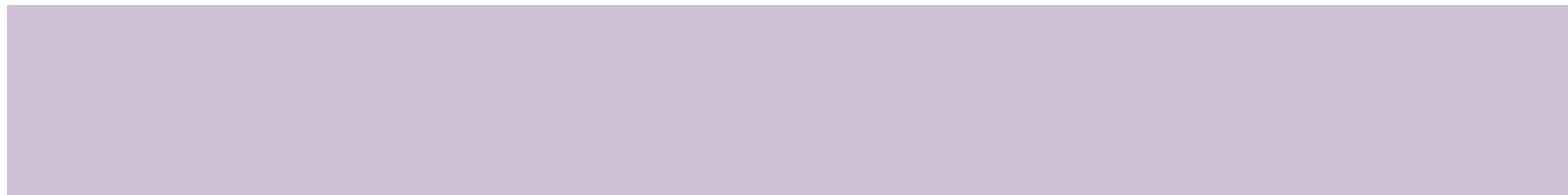
- Sorted Array



Shift 4 elements to right (4 copies)

- Sorted Double Linked List

(Search is slow, insert is fast)



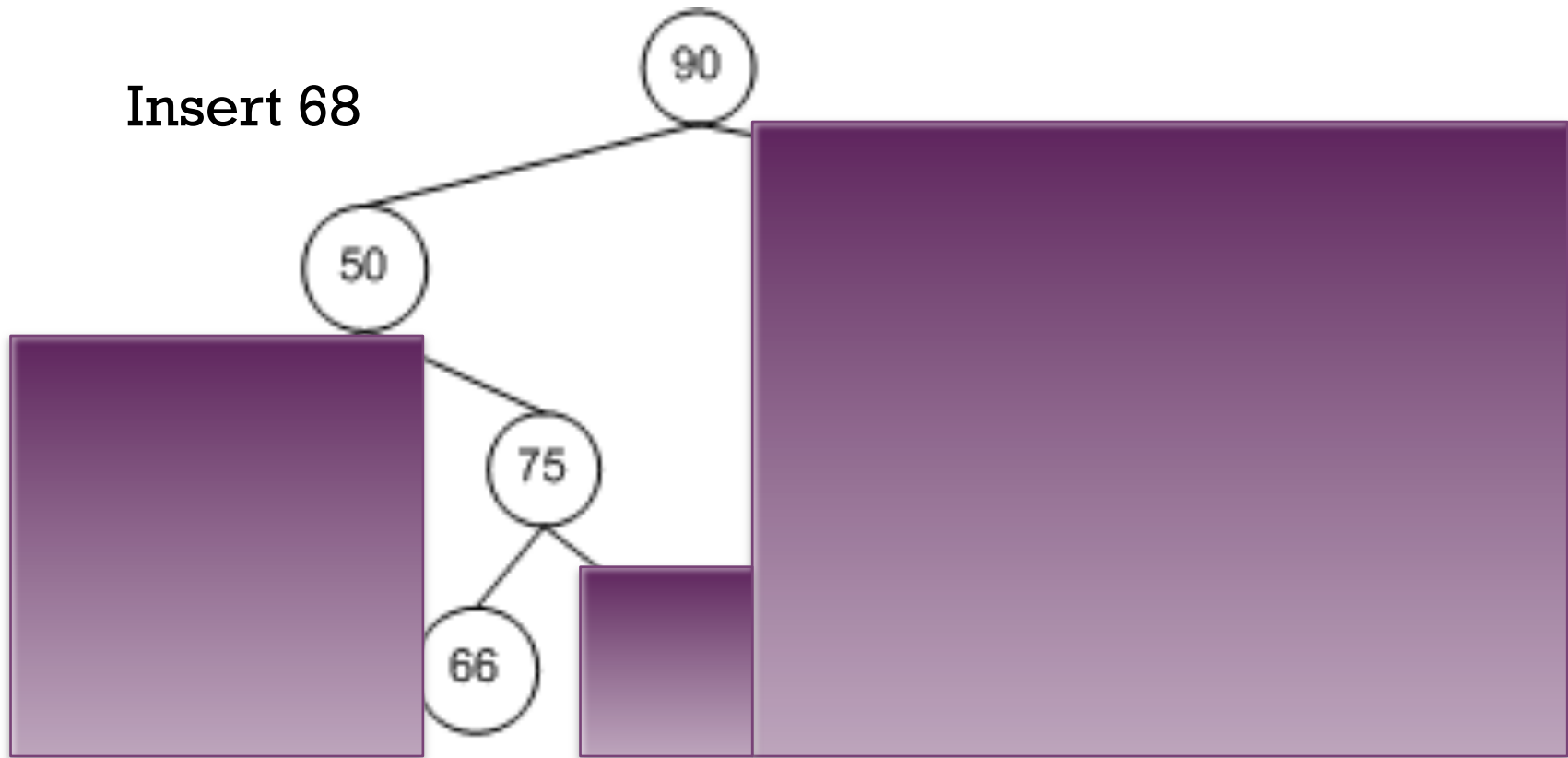
Can we have both fast search and fast insert?

# + An Efficient Data Structure

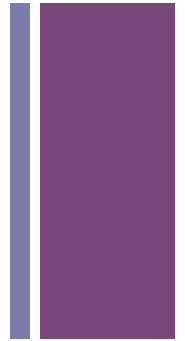


- Imagine a data structure that only needs at most  $O(\log n)$  comparisons to find an answer and  $O(\log n)$  actions to insert or remove a value.
- What would it look like?
  - For search: Each comparison would need to eliminate half of the remaining options.
  - For insertion/removal: The location of the value would need to be  $\log n$  steps from the initial starting place or cause  $\log n$  items to shift.

# + Will a Binary Search Tree work?

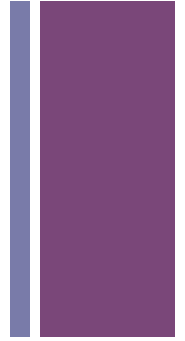


# + Implementation



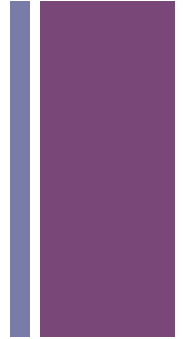
- add
- find
- min
- max
- successor
- predecessor
- remove

# + Add e



- If tree is empty
  - make a root node with e as its data
- else
  - `add(e, root);`

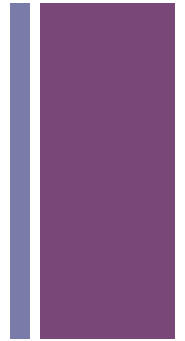
# + Add e, node



- if `e < node.data`
  - if (`node.left == null`)
    - make a left node with `e` as its data
  - else
    - `add(e, node.left)`
- else if `e > node.data`
  - if (`node.right == null`)
    - ...
- else
  - `return false // can't add equal items.`



# + Find e

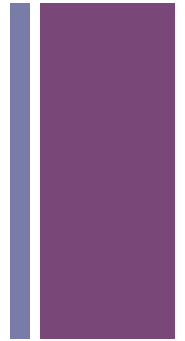


- If tree is empty
  - return null
- else
  - return find(e, root)
- find(e, node)
  - if e equals node.data
    - return node data
  - else if e < node.data
    - return find(e, node.left)
  - else
    - return find(e, node.right)

# + max()

[ note: min is similar using node.left instead of node.right ]

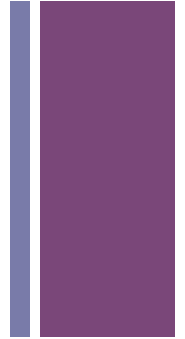
- If tree is empty
  - return null
- else
  - return max(root)
- max( node )
  - if node.right == null
    - return node data
  - else
    - return max(node.right)



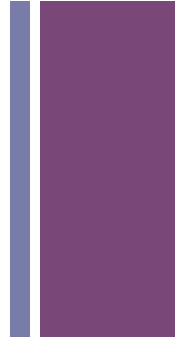
## + predecessor(node)

[ note: successor is similar using  
node.right instead of node.left]

- return max(node.left)

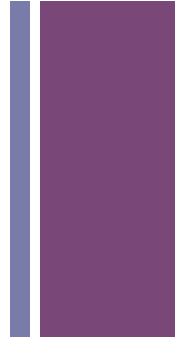


# + Traversal algorithms



- PreOrder(treeNode)
  - if treeNode is empty
    - done
  - else
    - "visit" treeNode
    - PreOrder(treeNode.left)
    - PreOrder(treeNode.right)
- Similarly for inOrder and postOrder
- Another example on board.

# + Exercise



- Get into groups
- do part 1, steps 1 to 3 from Assignment 6 in your group.